

8-4: MULTIPLYING SPECIAL CASES

Lesson Objectives:

- Finding the square of a binomial
- Finding the difference of two squares

$$\begin{array}{ll} (3x-7)^2 & (a-b)^2 \\ (3x-7)(3x-7) & (a-b)(a-b) \\ 9x^2 - 21x - 21x + 49 & a^2 - ab - ab + b^2 \\ 9x^2 - 42x + 49 & a^2 - 2ab + b^2 \end{array}$$

1

Finding the Square of a Binomial

$$(a+b)(a+b) \quad (a-b)(a-b)$$

The expressions $(a+b)^2$ and $(a-b)^2$ are squares of binomials. To square a binomial, you can use FOIL or the following shortcut.

RULE: THE SQUARE OF A BINOMIAL

$$(a+b)^2 = a^2 + 2ab + b^2$$

and

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$(a \pm b)^2 = a^2 \pm 2ab + b^2$$

The square of a binomial is the square of the first term, plus twice the product of the two terms, plus the square of the last term.

EXAMPLE 1: SQUARING A BINOMIAL

Simplify.

$$1. (x+4)^2 = x^2 + 2 \cdot x \cdot 4 + 4^2 = x^2 + 8x + 16$$

$$2. (y-3)^2 = y^2 - 2 \cdot y \cdot 3 + 3^2 = y^2 - 6y + 9$$

$$3. (y+11)^2 = y^2 + 2 \cdot y \cdot 11 + 11^2 = y^2 + 22y + 121$$

$$4. (3w-5)^2 = 9w^2 - 2 \cdot 3w \cdot 5 + 5^2 = 9w^2 - 30w + 25$$

Don't Do
 $9w^2 - 25$ X
 $9w^2 - 15w + 25$ X

$$5. (t+6)^2 = t^2 + 2 \cdot t \cdot 6 + 6^2 = t^2 + 12t + 36$$

$$6. (x-7)^2 = x^2 - 2 \cdot x \cdot 7 + 7^2 = x^2 - 14x + 49$$

$$7. (9c-8)^2 = 81c^2 - 2 \cdot 9c \cdot 8 + 8^2 = 81c^2 - 144c + 64$$

$$8. (3m+2n)^2 = 9m^2 + 2 \cdot 3m \cdot 2n + 4n^2 = 9m^2 + 12mn + 4n^2$$

$$9. (x^2+y^2)^2 = x^4 + 2x^2y^2 + y^4$$

$$10. (2x^2+y^2)^2 = 4x^4 + 4x^2y^2 + y^4$$

$$11. (y^2-4w^2)^2 = y^4 - 8y^2w^2 + 16w^4$$

$$12. (5x^4-3x^2)^2 = 25x^8 - 30x^6 + 9x^4$$

EXAMPLE 2: MENTAL MATH

Simplify in your mind.

$$13. 81^2 = (80+1)^2 = 6400 + 160 + 1 = 6561$$

$$14. 59^2 = (60-1)^2 = 3600 - 120 + 1 = 3481$$

$$15. 31^2 = (30+1)^2 = 900 + 60 + 1 = 961$$

$$16. 29^2$$

$$(30-1)^2$$

$$900 - 60 + 1$$

$$(841)$$

$$17. 98^2$$

$$(100-2)^2$$

$$10000 - 400 + 4$$

$$(9604)$$

$$18. 203^2$$

$$(200+3)^2$$

$$40000 + 1200 + 9$$

$$(41209)$$

2 Difference of Squares

The product of the sum and difference of the same two terms also produces a pattern.

$$(2x+7)(2x-7)$$

$$4x^2 + 14x - 14x - 49$$

$$(4x^2 - 49)$$

RULE: THE DIFFERENCE OF TWO SQUARES

$$(a+b)(a-b) = a^2 - b^2$$

The product of the sum and difference of the same two terms is the difference of their squares.

EXAMPLE 3: FINDING THE DIFFERENCE OF TWO SQUARES

Simplify.

$$19. (x+4)(x-4)$$

$$(x^2 - 16)$$

$$20. (3x-5)(3x+5)$$

$$(9x^2 - 25)$$

$$21. (p^4-8)(p^4+8)$$

$$(p^8 - 64)$$

$$22. (d+11)(d-11)$$

$$(d^2 - 121)$$

$$23. (c^2+8)(c^2-8)$$

$$(c^4 - 64)$$

$$24. (9v^3+w^4)(9v^3-w^4)$$

$$(81v^6 - w^8)$$

$$25. (x^2-2y)(x^2+2y)$$

$$(x^4 - 4y^2)$$

$$26. (3x+4)(3x+4)$$

$$(3x+4)^2$$

$$a^2 + 2ab + b^2$$

$$(9x^2 + 24x + 16)$$

EXAMPLE 4: MENTAL MATH

Simplify in your brains.

$$27. (18)(22)$$

$$(20-2)(20+2)$$

$$400 - 4$$

$$(396)$$

$$28. (19)(21)$$

$$(20-1)(20+1)$$

$$400 - 1$$

$$(399)$$

$$29. (59)(61)$$

$$(60-1)(60+1)$$

$$3600 - 1$$

$$(3599)$$

$$30. (87)(93)$$

$$(90-3)(90+3)$$

$$8100 - 9$$

$$(8091)$$

$$31. (96)(104)$$

$$(100-4)(100+4)$$

$$10000 - 16$$

$$(9984)$$

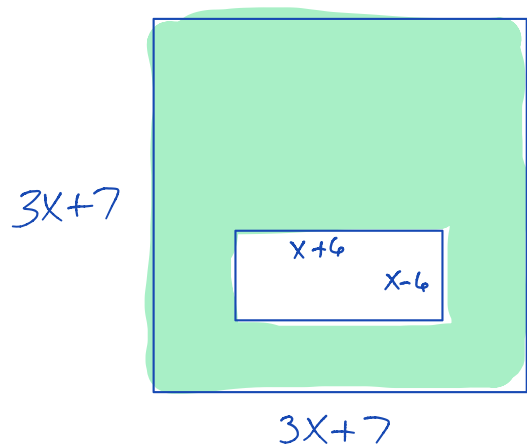
$$32. (33)(47)$$

$$(40-7)(40+7)$$

$$1600 - 49$$

$$(1551)$$

33. Find the area of the shaded region that is (eventually) drawn on the board.



$$\begin{aligned}
 & A_{\text{large}} - A_{\text{small}} \\
 & (3x+7)^2 - [(x+6)(x-6)] \\
 & \underline{9x^2 + 42x + 49} + \underline{[-x^2 + 36]} \\
 & \underline{8x^2 + 42x + 85}
 \end{aligned}$$

34. Simplify.

a) $(x+4)(x+3)$

$$\begin{aligned}
 & x^2 + \underline{3x} + \underline{4x} + 12 \\
 & \underline{x^2 + 7x + 12}
 \end{aligned}$$

b) $(x+4)(x-4)$

$$\underline{x^2 - 16}$$

c) $(x-4)^2$

$$\underline{x^2 - 8x + 16}$$

d) $(2x-7)(2x+7)$

$$\underline{4x^2 - 49}$$

e) $(2x-1)(2x+3)$

$$\begin{aligned}
 & 4x^2 + \underline{6x} - \underline{2x} - 3 \\
 & \underline{4x^2 + 4x - 3}
 \end{aligned}$$

f) $(2x+5)^2$

$$\underline{4x^2 + 20x + 25}$$

Due Wed

Name _____

8-4 Practice Worksheet

Period _____

Simplify each product.

1. $(x+4)^2$

2. $(3m+7)^2$

3. $(b-5)^2$

4. $(9j-2)^2$

5. $(a+8)(a-8)$

6. $(h+15)(h-15)$

7. $(k+5)(k-5)$

8. $(x-7y)^2$

9. $(6a+11b)^2$

10. $(y^5-9x^4)^2$

11. $(2d+7g)(2d-7g)$

12. _____

$(g^3-7h^2)(g^3+7h^2)$

Use mental math to find each product. Show the setup step.

13. 302^2

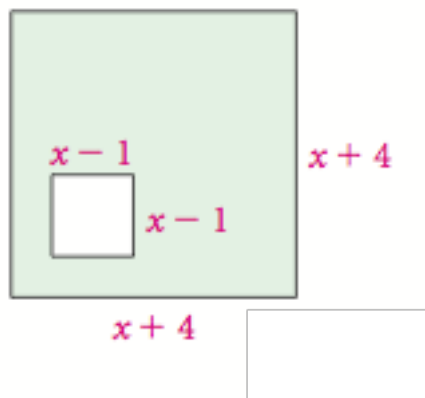
14. 499^2

15. $(197)(203)$

16. $(299)(301)$

Find an expression for the area of the shaded region.

17. $A_{\text{square}} = (\text{length of a side})^2$



MIXED REVIEW

Evaluate each expression for $x=3$, $y=-1$, and $z=2$.

18. $-xyz$

19. $-z^3 - 2z + z$

20. $y^2 - (-y)^2$

$$\text{Prob.} = \frac{\# \text{ favorable}}{\# \text{ possible}}$$

$$\text{Odds in favor} \\ \# \text{ favorable} : \# \text{ unfavorable}$$

$$\text{odds against} \\ \# \text{ unfavorable} : \# \text{ favorable}$$

Suppose you have a bag containing 3 red, 4 blue, 5 white, and 2 black marbles. You select one marble at random. Find each probability or odds.

21. $P(\text{not white})$

22. $P(\text{red or blue})$

23. $P(\text{orange})$

24. $P(\text{not black})$

$$\frac{9}{14}$$

25. odds in favor of red

26. odds against blue

27. odds against black or white

$$3:11$$

28. odds in favor of red, white, or blue

You have 8 red checkers and 8 black checkers in a bag. You choose two checkers. Find each probability.

29. $P(\text{red and red})$ with replacing

$$P(r) \cdot P(r)$$

30. $P(\text{red then black})$ without replacing

$$P(r) \cdot P(b \text{ after } r)$$

31. $P(\text{black and red})$ with replacing